

INSTRUCTOR GUIDANCE EXAMPLE: Week Four Discussion

Solving Quadratic Equations

#79 pg 637: Solve by Factoring

There is another way this problem could be solved (by **completing the square** which has already been done to it) but our instructions say to solve by **factoring**. This will require us to multiply out the left side and then subtract $9/4$ from both sides to leave the right side zero.

$$(p + \frac{1}{2})^2 = 9/4$$

$$p^2 + p + \frac{1}{4} = 9/4$$

$$p^2 + p - 2 = 0$$

$$(p + 2)(p - 1) = 0$$

$$p + 2 = 0 \quad \text{or} \quad p - 1 = 0$$

$$p = -2 \quad \text{or} \quad p = 1$$

$$\{-2, 1\}$$

First we need to expand the left side by FOIL.

Subtract $9/4$ from both sides.

Since $\frac{1}{4} - 9/4 = -8/4 = -2$ we now are free of the fractions.

Left side is **factored**.

Using the Zero Factor Property.

Our solutions.

Solution set presented.

$$\text{Check: } (p + \frac{1}{2})^2 = 9/4$$

$$(-2 + \frac{1}{2})^2 = 9/4$$

$$(-3/2)^2 = 9/4$$

$$9/4 = 9/4$$

$$(p + \frac{1}{2})^2 = 9/4$$

$$(1 + \frac{1}{2})^2 = 9/4$$

$$(3/2)^2 = 9/4$$

$$9/4 = 9/4$$

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$$-x^2 + x + 6 = 0$$

$$-1(x^2 - x - 6) = 0$$

$$x^2 - x - 6 = 0$$

$$(x - 3)(x + 2) = 0$$

$$x - 3 = 0 \quad \text{or} \quad x + 2 = 0$$

$$x = 3 \quad \text{or} \quad x = -2$$

$$\{-2, 3\}$$

Factor -1 out of all terms first.

Divide both sides by -1

Ready for **factoring**.

Left side is factored.

Using the Zero Factor Property.

Our solutions.

Solution set presented.

$$\text{Check: } -x^2 + x + 6 = 0$$

$$-(-2)^2 + (-2) + 6 = 0$$

$$-4 - 2 + 6 = 0$$

$$-6 + 6 = 0$$

$$0 = 0$$

$$-x^2 + x + 6 = 0$$

$$-(3)^2 + 3 + 6 = 0$$

$$-9 + 3 + 6 = 0$$

$$-6 + 6 = 0$$

$$0 = 0$$

#47 pg 646: Solve using **Quadratic Formula**

$$3y^2 + 2y - 4 = 0$$

$$a = 3, \quad b = 2, \quad c = -4 \quad \text{Discriminant is } b^2 - 4ac$$

which is $2^2 - 4(3)(-4) = 52$ so we have two real solutions.

$$y = \frac{-(2) \pm \sqrt{2^2 - 4(3)(-4)}}{2(3)}$$

All values put into the formula in parenthesis.

$$y = \frac{-2 \pm \sqrt{4 + 48}}{6}$$

Simplification begins.

$$y = \frac{-2 \pm \sqrt{52}}{6}$$

Need to simplify the radical next: $52 = 4 \cdot 13$

$$y = \frac{-2 \pm 2\sqrt{13}}{6}$$

$$y = \frac{-1 \pm \sqrt{13}}{3}$$

$$\{.869, -1.535\}$$

Both terms in the top and 6 have a factor of 2 which can be canceled out.

This is our solution set in radical form.

Our solution set presented as decimal approximations.

Using the Quadratic Formula will work on all types of quadratic equations, but factoring is quicker and easier if it is a possible choice for the equation.